

Paper Reference(s)

**6683/01**

# **Edexcel GCE**

## **Statistics S1**

### **Advanced Level**

**Friday 14 January 2011 – Morning**

**Time: 1 hour 30 minutes**

**Materials required for examination**

Mathematical Formulae (Pink)

**Items included with question papers**

Nil

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulas stored in them.**

#### **Instructions to Candidates**

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In the boxes on the answer book, write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Statistics S2), the paper reference (6684), your surname, other name and signature.

Values from the statistical tables should be quoted in full. When a calculator is used, the answer should be given to an appropriate degree of accuracy.

#### **Information for Candidates**

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A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

This paper has 8 questions.

The total mark for this paper is 75.

#### **Advice to Candidates**

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You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

1. A random sample of 50 salmon was caught by a scientist. He recorded the length  $l$  cm and weight  $w$  kg of each salmon.

The following summary statistics were calculated from these data.

$$\sum l = 4027 \quad \sum l^2 = 327\,754.5 \quad \sum w = 357.1 \quad \sum lw = 29\,330.5 \quad S_{ww} = 289.6$$

- (a) Find  $S_{ll}$  and  $S_{lw}$ . (3)
- (b) Calculate, to 3 significant figures, the product moment correlation coefficient between  $l$  and  $w$ . (2)
- (c) Give an interpretation of your coefficient. (1)
- 

2. Keith records the amount of rainfall, in mm, at his school, each day for a week. The results are given below.

2.8    5.6    2.3    9.4    0.0    0.5    1.8

Jenny then records the amount of rainfall,  $x$  mm, at the school each day for the following 21 days. The results for the 21 days are summarised below.

$$\sum x = 84.6$$

- (a) Calculate the mean amount of rainfall during the whole 28 days. (2)

Keith realises that he has transposed two of his figures. The number 9.4 should have been 4.9 and the number 0.5 should have been 5.0.

Keith corrects these figures.

- (b) State, giving your reason, the effect this will have on the mean. (2)
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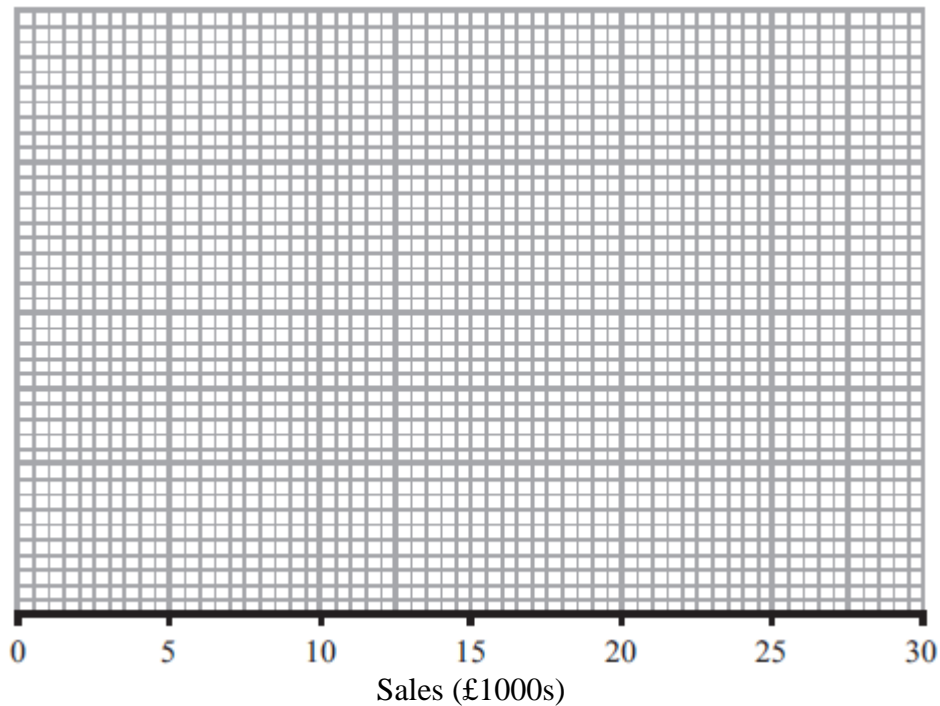
3. Over a long period of time a small company recorded the amount it received in sales per month. The results are summarised below.

	Amount received in sales (£1000s)
Two lowest values	3, 4
Lower quartile	7
Median	12
Upper quartile	14
Two highest values	20, 25

An outlier is an observation that falls either  $1.5 \times$  interquartile range above the upper quartile or  $1.5 \times$  interquartile range below the lower quartile.

- (a) On the graph paper below, draw a box plot to represent these data, indicating clearly any outliers.

(5)



- (b) State the skewness of the distribution of the amount of sales received. Justify your answer. (2)
- (c) The company claims that for 75 % of the months, the amount received per month is greater than £10 000. Comment on this claim, giving a reason for your answer. (2)

4. A farmer collected data on the annual rainfall,  $x$  cm, and the annual yield of peas,  $p$  tonnes per acre.

The data for annual rainfall was coded using  $v = \frac{x-5}{10}$  and the following statistics were found.

$$S_{vv} = 5.753 \quad S_{pv} = 1.688 \quad S_{pp} = 1.168 \quad \bar{p} = 3.22 \quad \bar{v} = 4.42$$

- (a) Find the equation of the regression line of  $p$  on  $v$  in the form  $p = a + bv$ . (4)

- (b) Using your regression line estimate the annual yield of peas per acre when the annual rainfall is 85 cm. (2)
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5. On a randomly chosen day, each of the 32 students in a class recorded the time,  $t$  minutes to the nearest minute, they spent on their homework. The data for the class is summarised in the following table.

Time, $t$	Number of students
10 – 19	2
20 – 29	4
30 – 39	8
40 – 49	11
50 – 69	5
70 – 79	2

- (a) Use interpolation to estimate the value of the median. (2)

Given that

$$\sum t = 1414 \quad \text{and} \quad \sum t^2 = 69\,378,$$

- (b) find the mean and the standard deviation of the times spent by the students on their homework. (3)
- (c) Comment on the skewness of the distribution of the times spent by the students on their homework. Give a reason for your answer. (2)
-

6. The discrete random variable  $X$  has the probability distribution

$x$	1	2	3	4
$P(X = x)$	$k$	$2k$	$3k$	$4k$

(a) Show that  $k = 0.1$  (1)

Find

(b)  $E(X)$  (2)

(c)  $E(X^2)$  (2)

(d)  $\text{Var}(2 - 5X)$  (3)

Two independent observations  $X_1$  and  $X_2$  are made of  $X$ .

(e) Show that  $P(X_1 + X_2 = 4) = 0.1$  (2)

(f) Complete the probability distribution table for  $X_1 + X_2$ . (2)

$y$	2	3	4	5	6	7	8
$P(X_1 + X_2 = y)$	0.01	0.04	0.10		0.25	0.24	

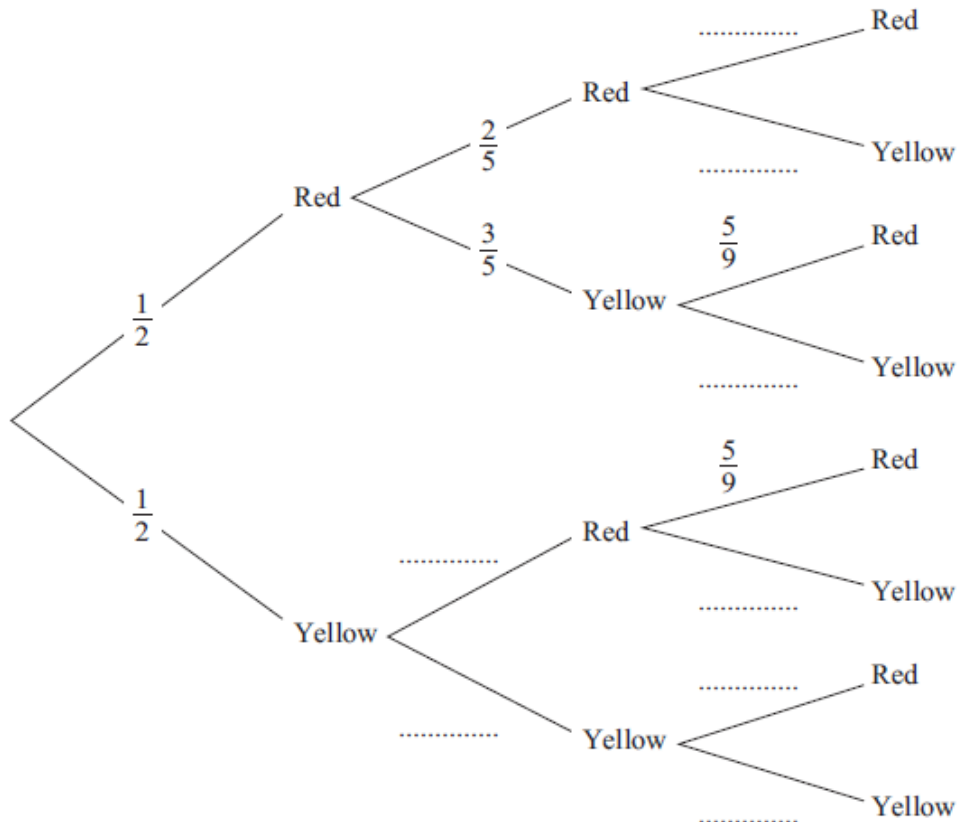
(g) Find  $P(1.5 < X_1 + X_2 \leq 3.5)$  (2)

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7. The bag  $P$  contains 6 balls of which 3 are red and 3 are yellow.  
 The bag  $Q$  contains 7 balls of which 4 are red and 3 are yellow.  
 A ball is drawn at random from bag  $P$  and placed in bag  $Q$ . A second ball is drawn at random from bag  $P$  and placed in bag  $Q$ .  
 A third ball is then drawn at random from the 9 balls in bag  $Q$ .

The event  $A$  occurs when the 2 balls drawn from bag  $P$  are of the same colour.  
 The event  $B$  occurs when the ball drawn from bag  $Q$  is red.

- (a) Copy and complete the tree diagram shown below.



(4)

- (b) Find  $P(A)$ .

(3)

- (c) Show that  $P(B) = \frac{5}{9}$ .

(3)

- (d) Show that  $P(A \cap B) = \frac{2}{9}$ .

(2)

- (e) Hence find  $P(A \cup B)$ .

(2)

- (f) Given that all three balls drawn are the same colour, find the probability that they are all red.

(3)

8. The weight,  $X$  grams, of soup put in a tin by machine  $A$  is normally distributed with a mean of 160 g and a standard deviation of 5 g.

A tin is selected at random.

- (a) Find the probability that this tin contains more than 168 g. (3)

The weight stated on the tin is  $w$  grams.

- (b) Find  $w$  such that  $P(X < w) = 0.01$ . (3)

The weight,  $Y$  grams, of soup put into a carton by machine  $B$  is normally distributed with mean  $\mu$  grams and standard deviation  $\sigma$  grams.

- (c) Given that  $P(Y < 160) = 0.99$  and  $P(Y > 152) = 0.90$ , find the value of  $\mu$  and the value of  $\sigma$ . (6)

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**TOTAL FOR PAPER: 75 MARKS**

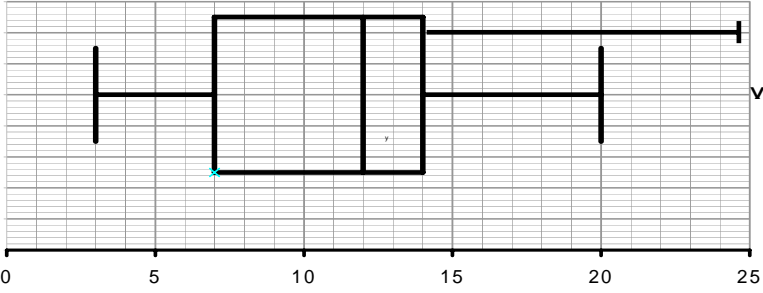
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**January 2011  
Statistics S1 6683  
Mark Scheme**

Question Number	Scheme	Marks
1.		
(a)	$S_{ll} = 327754.5 - \frac{4027^2}{50} = 3419.92$ $S_{lw} = 29330.5 - \frac{357.1 \times 4027}{50} = 569.666$	M1 A1 A1 (3)
(b)	$r = \frac{569.666}{\sqrt{3419.92 \times 289.6}} = 0.572$	awrt 0.572 or 0.573 M1 A1 (2)
(c)	As the length of the salmon increases the weight increases	B1ft (1) <b>[6]</b>
<b>Notes</b>		
(a)	M1 for at least one correct expression 1 <sup>st</sup> A1 for $S_{ll} =$ awrt 3420 (Condone $S_{xx} = \dots$ or even $S_{yy} = \dots$ ) 2 <sup>nd</sup> A1 for $S_{lw} =$ awrt 570 (Condone $S_{xy} = \dots$ )	
(b)	M1 for attempt at correct formula. Must have their $S_{ll}$ , $S_{lw}$ and given $S_{ww}$ in the correct places If $S_{ll}$ , $S_{lw}$ are correct and an answer of awrt 0.57 is seen then award M1A0 M0 for $\frac{29330.5}{\sqrt{327754.5 \times 289.6}}$	
(c)	B1ft for a comment mentioning “length” and “weight”, not just $l$ and $w$ , and the idea of longer salmon weighing more. e.g. “positive correlation between weight and length” is B0 since the idea of positive correlation is not explained. Allow “larger” instead of “heavier” or “longer” Ignore any spurious values mentioned such as 0.572 If their $r$ is negative (but must be $r > -1$ ) ft an appropriate comment. Condone $r > 1$ if comment is correct. If $ r  < 0.4$ allow a comment of no or little relationship between weight and length but for $0 < r < 0.4$ the printed answer is still acceptable too.  Treat mention of “skewness” as ISW if a correct interpretation is given	



Question Number	Scheme	Marks
2.  (a)	$2.8 + 5.6 + 2.3 + 9.4 + 0.5 + 1.8 + 84.6 = 107$ mean = $107 / 28 (= 3.821\dots)$	M1 A1 (2)
(b)	It will have no effect since one is 4.5 under what it should be and the other is 4.5 above what it should be.	B1 dB1 (2) [4]
<b>Notes</b>		
(a)	M1 for a clear attempt to add the two sums. Accept a full expression or $2.8 + 5.6 + \dots + 84.6 = x$ where $100 < x < 110$ i.e. seeing at least two correct terms of Keith's and the 84.6 with a slip. A1 for awrt 3.8 (Condone 1 dp/2sf here since data is given to 1 dp or 2 sf) Accept $\frac{107}{28}$ or $3\frac{23}{28}$ or any exact equivalent <b>Correct answer implies M1A1</b>	
(b)	1 <sup>st</sup> B1 for clearly stating that it will have no effect. ("roughly the same" is B0 B0) 2 <sup>nd</sup> dB1 for a supporting reason that mentions the fact that the increase and decrease are the same and gives some numerical value(s) to support this. e.g. Sum of Keith's observations is still 22.4 ( or mean is still 3.2) <u>or</u> Sum is still 107 <u>or</u> $9.4 - 4.9 = 5 - 0.5$ (o.e.) This second B1 is dependent on their saying there is no effect so BOB1 is not possible.	

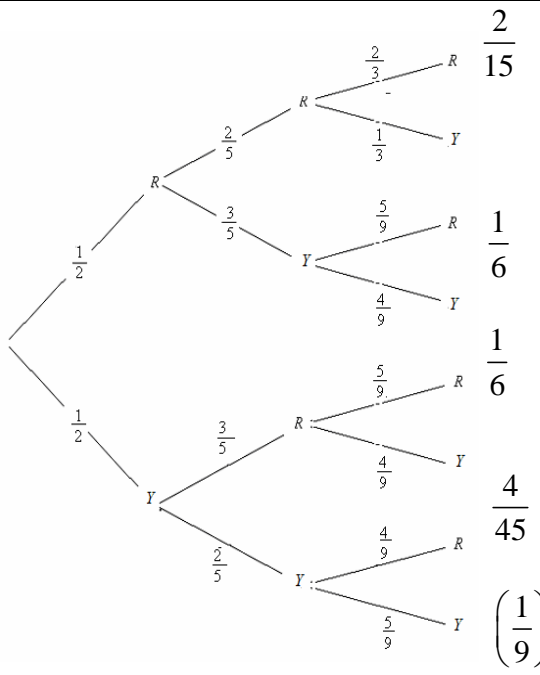
Question Number	Scheme	Marks
3. (a)	<p><b>Outliers</b>  <math>14 + 1.5 \times (14 - 7) = 24.5</math>  <math>7 - 1.5 \times (14 - 7) = -3.5</math></p> <p><b>Outlier 25</b>  either upper limit acceptable on diagram</p>  <p style="text-align: right;">Sales in £'000</p>	M1 A1  M1 A1ft B1   (5)
(b)	Since $Q_3 - Q_2 < Q_2 - Q_1$ . Allow written explanation negatively skew	B1 dB1  (2)
(c)	not true since the lower quartile is 7000 and therefore 75% above 7000 not 10000 or 10 is inside the box or any other sensible comment	B1 dB1  (2) [9]
<b>Notes</b>		
(a)	<p><b>A fully correct box-plot (either version) with no supporting work scores 5/5. Otherwise read on</b></p> <p>1<sup>st</sup> M1 for at least one correct calculation seen  1<sup>st</sup> A1 for 24.5 and -3.5 (or just negative noted) seen. May be read off the graph.  If both values are seen but no calculation is given then M1A1, one value M1A0.  2<sup>nd</sup> M1 for a box with an upper and a lower whisker(s) with at least 2 correct values (condone no median marked)  2<sup>nd</sup> A1ft for 3, 7, 12, 14 and 20 or 24.5 in appropriate places and readable off their scale  If <u>both</u> upper whiskers are seen A0  Apply ft for their <u>whiskers</u> being compatible with their <u>outlier limits</u>  e.g. if their lower limit is + 3.5 then a lower whisker ending at 4 or 3.5 is OK  B1 for only one outlier appropriately marked at 25</p> <p style="text-align: center;"><b>Apply + 0.5 square accuracy for diagram</b></p>	
(b)	1 <sup>st</sup> B1 for $Q_3 - Q_2 < Q_2 - Q_1$ statement or an equivalent statement in words Use of $Q_3 - Q_2 < Q_2 - Q_1$ does not require differences to be seen. 2 <sup>nd</sup> dB1 for “negative skew” dependent on suitable reason given above. “correlation” is B0 “positive skew” with a supporting argument based on whiskers can score B1B1 e.g. “right hand whisker is longer than LH one so positive skew” $Q_3 - Q_2 < Q_2 - Q_1$ followed by “positive skew” is B1B0	
(c)	1 <sup>st</sup> B1 for rejecting the company’s claim 2 <sup>nd</sup> dB1 for an appropriate supporting reason. Dependent on rejecting company’s claim.	

Question Number	Scheme	Marks
4. (a)	$b = \frac{1.688}{5.753} = 0.293$ $a = 3.22 - 4.42 \times 0.293 = 1.9231\dots$ $p = 1.92 + 0.293v$	M1A1  M1 A1  (4)
(b)	$v = \frac{85-5}{10} = 8$ $p = 1.92 + 0.293 \times 8 = 4.3$ <p style="text-align: right;"><b>(awrt 4.3)</b></p>	M1  A1  (2) [6]
<b>Notes</b>		
(a)	<b>Can ignore (a) and (b) labels here</b>	
	<p>1<sup>st</sup> M1 for a correct expression for <math>b</math>. <math>\frac{1.688}{1.168}</math> is M0</p> <p>1<sup>st</sup> A1 for awrt 0.29</p> <p>2<sup>nd</sup> M1 for use of <math>a = \bar{p} - b\bar{v}</math> follow through their value of <math>b</math> (or even just the letter <math>b</math>)</p> <p>2<sup>nd</sup> A1 for a complete equation with <math>a =</math> awrt 1.92 and <math>b =</math> awrt 0.293  <math>y</math> or <math>p = 1.92 + 0.293x</math> is A0            Correct answer with no working is 4/4</p>	
(b)	<p>M1 for an attempt to find the value of <math>v</math> when <math>x = 85</math> ( at least 2 correct terms in <math>\pm \frac{85-5}{10}</math> )</p> <p>or for an attempt to find an equation for <math>p</math> in terms of <math>x</math> and using <math>x = 85</math></p> <p>Attempt at equation of <math>p</math> in <math>x</math> requires <math>p = 1.92 + 0.293 \frac{(x-5)}{10}</math></p> <p>A1 for awrt 4.3 (award when first seen and apply ISW)            N.B. <math>p = 1.92 + 0.293 \times 85</math> (o.e.) is M0A0</p>	

Question Number	Scheme	Marks
5.		
(a)	Median = $32/2 = 16^{\text{th}}$ term (16.5) $\frac{x - 39.5}{49.5 - 39.5} = \frac{16 - 14}{25 - 14}$ or $x = 39.5 + \left(\frac{2}{11} \times 10\right)$ Median = 41.3 (use of $n + 1$ gives 41.8) <b>(awrt 41.3)</b>	M1 A1 (2)
(b)	Mean = $\frac{1414}{32} = 44.1875$ <b>(awrt 44.2)</b> Standard deviation = $\sqrt{\frac{69378}{32} - \left(\frac{1414}{32}\right)^2}$ $= 14.7$ (or $s = 14.9$ )	B1 M1 A1 (3)
(c)	mean > median therefore <u>positive skew</u>	B1ft B1ft (2) <b>[7]</b>
<b>Notes</b>		
(a)	M1 for an attempt to use interpolation to find the median. Condone use of 39 or 40 for 39.5 e.g. allow $39 + \frac{2}{11} \times 10$ (o.e.) or $40 + \frac{2}{11} \times 10$ (o.e.) to score M1A0 but must have the 10 A1 for awrt 41.3 (or awrt 41.8 if using $(n + 1)$ )	
(b)	B1 for awrt 44.2 M1 for a correct expression including square root. (Allow ft of their mean) A1 for awrt 14.7 (If using $s$ for awrt 14.9) You may see $\sum t = 1339 \rightarrow \bar{t} = 41.8$ and $\sum t^2 = 62928 \rightarrow \sigma 14.7$ or $s = 14.9$ this scores B0 for the mean but can score M1 for a correct st.dev expression and A1 for ans. <b>Correct answer only in (a) and (b) can score full marks but check <math>(n + 1)</math> case in (a)</b>	
(c)	1 <sup>st</sup> B1ft for a correct comparison of their mean and their median (may be in a formula) Calculating median – mean as negative is OK for this B1 but must say +ve skew for 2 <sup>nd</sup> B1 Only allow comparison to be $\approx 0$ if $ \text{mean} - \text{median}  \leq 0.5$ 2 <sup>nd</sup> B1ft for a correct description of skewness <u>based on their values of mean and median.</u> ft their values for mean and median not their previous calculation/comparison Must be compatible with their previous comparison (if they have one) “Positive skew” with no reason is B0B1 provided you can see their values that imply that. Description should be “positive” or “negative” or “no” skew or “symmetric” “Positive correlation” is B0	
Quartiles	1 <sup>st</sup> B1ft if $Q_1 = \text{awrt } 32$ <u>and</u> $Q_3 = \text{awrt } 49$ seen and a correct comparison made. ft $Q_2$ 2 <sup>nd</sup> B1ft if $Q_1 = \text{awrt } 32$ <u>or</u> $Q_3 = \text{awrt } 49$ seen and a correct description based on their quartiles and their comparison is made. (Should get “negative skew”)	

Question Number	Scheme	Marks																
6.																		
(a)	$k + 2k + 3k + 4k = 1$ or $10k = 1$ $k = 0.1$ (*) [allow verification with a comment e.g. "so $k = 0.1$ "]	B1cso (1)																
(b)	$E(X) = 1 \times 0.1 + 2 \times 0.2 + 3 \times 0.3 + 4 \times 0.4 = 3$	M1 A1 (2)																
(c)	$E(X^2) = 1 \times 0.1 + 4 \times 0.2 + 9 \times 0.3 + 16 \times 0.4 = 10$	M1 A1 (2)																
(d)	$\text{Var}(X) = 10 - 9 (= 1)$ $\text{Var}(2 - 5X) = 5^2 \text{Var}(X) = 25$	M1 M1 A1 (3)																
(e)	$P(1,3) + P(2,2) = 2 \times 0.1 \times 0.3 + 0.2 \times 0.2 = 0.1$ (*)	M1 A1cso (2)																
(f)	<table border="1"> <tr> <td><math>X_1 + X_2</math></td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> </tr> <tr> <td><math>p</math></td> <td>0.01</td> <td>0.04</td> <td>0.1</td> <td><b>0.2</b></td> <td>0.25</td> <td>0.24</td> <td><b>0.16</b></td> </tr> </table>	$X_1 + X_2$	2	3	4	5	6	7	8	$p$	0.01	0.04	0.1	<b>0.2</b>	0.25	0.24	<b>0.16</b>	B1 B1 (2)
$X_1 + X_2$	2	3	4	5	6	7	8											
$p$	0.01	0.04	0.1	<b>0.2</b>	0.25	0.24	<b>0.16</b>											
(g)	$P(2) + P(3) = 0.05$	M1A1 (2) [14]																

Question Number	Scheme	Marks
<b>Notes</b>		
(a)	B1 for a clear attempt to use sum of probabilities = 1. Must see previous line as well as $k = 0.1$ <b>A correct expression for <math>E(X)</math> or <math>E(X^2)</math> that is later divided by 4 scores M0</b>	
(b)	M1 for a completely correct expression. May be implied by correct answer of 3 or $30k$ A1 for 3 only.	
(c)	M1 for a completely correct expression. May be implied by correct answer of 10 or $100k$ A1 for 10 only. [ For $E(X^2) = 0.1 + 0.8 + 2.7 + 6.4 - 9 = 1$ scores M0A0 but accept this as $\text{Var}(X)$ in (d)]	
(d)	1 <sup>st</sup> M1 for using $\text{Var}(X) = E(X^2) - E(X)^2$ , f.t their values from (b) and (c) Allow this mark for $\text{Var}(X) = 10 - 9$ or better. May be implied if this is seen in (c). 2 <sup>nd</sup> M1 for $5^2 \text{Var}(X)$ or $25\text{Var}(X)$ can f.t. their $\text{Var}(X)$ . Allow $-5^2$ if it later becomes $+25$ A1 for 25 only. Dependent upon both Ms Forming distribution for $Y = 2 - 5X$ gets M1 for $E(Y^2) = 194$ then M1A1 for $194 - 169 = 25$	
(e)	M1 for correctly identifying (1, 3) <u>or</u> (3, 1) <u>and</u> (2, 2) as required cases ( $3k^2 + 4k^2$ or better) A1 cso for 0.1 only but must see evidence for M1	
(f)	1 <sup>st</sup> B1 for 0.2 correctly assigned. May be in table. 2 <sup>nd</sup> B1 for 0.16 correctly assigned. May be in table	
(g)	M1 for $P(2) + P(3)$ . May be implied by correct answer of 0.05 A1 for 0.05 only. <b>Correct answer only can score full marks in parts (b), (c), (f) and (g)</b>	

Question Number	Scheme	Marks
7. (a)	 <p style="text-align: right;">       both <math>\frac{2}{3}, \frac{1}{3}</math>        B1          B1          both <math>\frac{3}{5}, \frac{2}{5}</math>        B1          all three of <math>\frac{4}{9}, \frac{4}{9}, \frac{5}{9}</math>        B1        (4)     </p>	
(b)	$P(A) = P(RR) + P(YY) = \frac{1}{2} \times \frac{2}{5} + \frac{1}{2} \times \frac{2}{5} = \frac{2}{5}$	B1 for $\frac{1}{2} \times \frac{2}{5}$ (oe) seen at least once B1 M1 A1 (3)
(c)	$P(B) = P(RRR) + P(RYR) + P(YRR) + P(YYR)$ $\left(\frac{1}{2} \times \frac{2}{5} \times \frac{2}{3}\right) + \left(\frac{1}{2} \times \frac{3}{5} \times \frac{5}{9}\right) + \left(\frac{1}{2} \times \frac{3}{5} \times \frac{5}{9}\right) + \left(\frac{1}{2} \times \frac{2}{5} \times \frac{4}{9}\right) = \frac{5}{9} \quad (*)$	M1 for at least 1 case of 3 balls identified. (Implied by 2 <sup>nd</sup> M1) M1 M1, A1cso (3)
(d)	$P(A \cap B) = P(RRR) + P(YYR)$ $= \left(\frac{1}{2} \times \frac{2}{5} \times \frac{2}{3}\right) + \left(\frac{1}{2} \times \frac{2}{5} \times \frac{4}{9}\right) = \frac{2}{9} \quad (*)$	M1 for identifying both cases and + probs. may be implied by correct expressions M1 A1cso (2)
(e)	$P(A \cup B) = P(A) + P(B) - P(A \cap B)$ $= \frac{2}{5} + \frac{5}{9} - \frac{2}{9} = \frac{11}{9}$	Must have some attempt to <u>use</u> M1 A1cao (2)

Question Number	Scheme	Marks
(f)	$\frac{P(RRR)}{P(RRR) + P(YYY)} = \frac{\frac{1}{2} \times \frac{2}{5} \times \frac{2}{3}}{\left(\frac{1}{2} \times \frac{2}{5} \times \frac{2}{3}\right) + \left(\frac{1}{2} \times \frac{2}{5} \times \frac{5}{9}\right)} = \frac{6}{11}$	<div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;">           Probabilities must come from the product of 3 probs. from their tree diagram.         </div> M1 A1ft A1 cao  (3)  [17]
<b>Notes</b>		
(b)	M1 for both cases, and +, attempted, ft their values from tree diagram. May be 4 cases of 3 balls.	
(c)	2 <sup>nd</sup> M1 for all 4 correct expressions, ft their values from tree diagram. A1 is cso	
(e)	M1 for clear attempt to <u>use</u> the correct formula, must have some correct substitution. ft their (b)	
(f)	M1 for identifying the correct probabilities and forming appropriate fraction of probs. 1 <sup>st</sup> A1ft for a correct expression using probabilities from their tree <b>Accept exact decimal equivalents. Correct answer only is full marks except in (c) and (d)</b>	



Question Number	Scheme	Marks
8.		
(a)	$P(X > 168) = P\left(Z > \frac{168-160}{5}\right)$ $= P(Z > 1.6)$ $= 0.0548$	M1 A1 A1 <b>awrt 0.0548</b> (3)
(b)	$P(X < w) = P\left(Z < \frac{w-160}{5}\right)$ $\frac{w-160}{5} = -2.3263$ $w = 148.37$	M1 B1 A1 <b>awrt 148</b> (3)
(c)	$\frac{160 - \mu}{\sigma} = 2.3263$ $\frac{152 - \mu}{\sigma} = -1.2816$ $160 - \mu = 2.3263\sigma$ $152 - \mu = -1.2816\sigma$ $8 = 3.6079\sigma$ $\sigma = 2.21\dots$ $\mu = 154.84\dots$	M1 B1 B1 M1 A1 A1 <b>awrt 2.22</b> <b>awrt 155</b> (6) [12]
<b>Notes</b>		
(a)	M1 for an attempt to standardize 168 with 160 and 5 i.e. $\pm\left(\frac{168-160}{5}\right)$ or implied by 1.6 1 <sup>st</sup> A1 for $P(Z > 1.6)$ or $P(Z < -1.6)$ ie $z = 1.6$ and a correct inequality or 1.6 on a shaded diagram <b>Correct answer to (a) implies all 3 marks</b>	
(b)	M1 for attempting $\pm\left(\frac{w-160}{5}\right) =$ recognizable $z$ value ( $ z  > 1$ ) B1 for $z = \pm 2.3263$ or better. Should be $z = \dots$ or implied so: $1 - 2.3263 = \frac{w-160}{5}$ is M0B0 A1 for awrt 148. This may be scored for other $z$ values so M1B0A1 is possible <b>For awrt 148 only with no working seen award M1B0A1</b>	
(c)	M1 for attempting to standardize 160 or 152 with $\mu$ and $\sigma$ (allow $\pm$ ) <u>and</u> equate to $z$ value ( $ z  > 1$ ) 1 <sup>st</sup> B1 for awrt $\pm 2.33$ or $\pm 2.32$ seen 2 <sup>nd</sup> B1 for awrt $\pm 1.28$ seen 2 <sup>nd</sup> M1 for attempt to solve their two linear equations in $\mu$ and $\sigma$ leading to equation in just one variable 1 <sup>st</sup> A1 for $\sigma =$ awrt 2.22 . Award when 1 <sup>st</sup> seen 2 <sup>nd</sup> A1 for $\mu =$ awrt 155. Correct answer only for part (c) can score all 6 marks. NB $\sigma = 2.21$ commonly comes from $z = 2.34$ and usually scores M1B0B1M1A0A1 <b>The A marks in (c) require both M marks to have been earned</b>	